Information evening based around the teaching and progression of multiplication and division across KS1 and KS2

Can you solve this problem?

Aunt Sophie has $3 p$ and 8 p stamps only.
It will cost 73 p to post a parcel.
How many of each type of stamp should she put on the parcel?



Can you work out the missing numbers?
Which skills and knowledge have you used to solve this puzzle

## Aims of the evening:

- Look at how multiplication and division is taught in the classroom through a CPA approach (Concrete - PictorialAbstract)
- Look at the the concrete resources/manipulatives that we use at school to support mathematical teaching and learning.
- How to support your children at home with their maths learning including the learning of times tables.


## Calculation: Multiplication

Key language: double, times, multiplied by, product, groups of, lots of, equal groups, arrays, factor, multiple, partition, commutative, column, value, multiple. multiplicand

Key representations: place value counters, base 10, bead strings, multilink, counters, Numicon, bar model, number line


| Arrays to show commutativity: | $\begin{gathered} 3 \times 4=4 \times 3 \\ 4+4+4=3+3+3+3 \end{gathered}$ | $\begin{gathered} 3 \times 4=4 \times 3 \\ 4+4+4=3+3+3+3 \end{gathered}$ | 'I can see 3 groups of 4 and I can see 4 groups of 3.' <br> '3 times 4 can represent 3 groups of 4. <br> It can also represent 4 times 3.' <br> 'If there are $\qquad$ equal groups, we can use the $\qquad$ times table.' |
| :---: | :---: | :---: | :---: |
| Partition to multiply: $3 \times 15=$ <br> becomes | $3 \times 15=$15 15 15 <br> $?$   <br> ? | $\begin{gathered} 3 \times 15= \\ 3 \times 10=30 \\ 3 \times 5=15 \\ 30+15=45 \end{gathered}$$x$ 10 5 <br> 3 30 15 | '15 is equal to 10 plus 5 . <br> So 3 times 15 is equal to 3 times 10 plus 3 times 5 .' |

## Calculation: Division

Key language: share, group, divide, divided by, half, equal, dividend, divisor, quotient, factor, multiple, remainder, dividend
Key representations: place value counters, base 10, bead strings, multilink, counters, Numicon, bar model, number line



https://www.oughtringtoncps.co.uk/page/maths/19169

## What does Maths look like?



## CPA Approach: Concrete, Pictorial, Abstract

## Concrete

Concrete resources (also referred to as manipulatives) are objects or physical resources that children can handle and manipulate to aid their understanding of different maths concepts. Children are able to 'see' the Maths and make sense of what is happening.


Bead strings
Numicon


Ten frames


Place value counters
Base 10

## Pictorial

Once children are confident with a concept using concrete resources, they progress to drawing pictorial representations or quick sketches of the objects. By doing this, they are no longer manipulating the physical resources, but are still benefiting from the visual support the resources provide.


Part whole model


## Abstract

Once children have a secure understanding of the concept through the use of concrete resources and visual images, they are then able to move on to the abstract.

## Why is C-P-A so important?

- In the past, children were taught procedures, but not why or how the procedure worked. In other words, children learnt the methods to get to an answer, without any understanding of the maths behind each method or procedure.
- While there are children who are able to access the maths through just learning a procedure by rote, many others have great difficulty coping with the abstract nature of it.
- Teaching methods without meaning leads to misconceptions, errors and difficulties in retaining the methods. Once children can actually 'see' the maths, they are much more likely to understand and accurately remember the methods.


## Multiplication/division - an overview of skills in different year groups.

| Year 1 | Count in multiples of 2,5 and 10. <br> Recall and use all doubles to 10 and corresponding halves. |
| :--- | :--- |
| Year 2 | Recall and use multiplication and division facts for 2,5, and 10 times <br> tables. |
| Year 3 | Recall and use multiplication and division facts for 3,4 and 8 times <br> tables. |
| Year 4 | Recall and use multiplication and division facts for $6,9,7,11$ and 12 <br> times tables. <br> It is the expectation that children will know all of their multiplication <br> and division facts up to $12 \times 12$ |
| Year 5 | Revision of all multiplication and division facts up to $12 \times 12$ <br> Year 6Revision of all multiplication and division facts up to $12 \times 12$ |

NC - Mathematics programmes of study: key stages 1 and 22013

Factual fluency progression

|  | Year 1 | Year 2 | Year 3 | Year 4 | Year 5 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Additive <br> factual <br> fluency | Addition and <br> subtraction within 10. | Addition and <br> subtraction across <br> 10. | Secure and maintain <br> fluency in addition <br> and subtraction <br> within and across 10, <br> through continued <br> practice. |  |  |
| Multiplicative <br> factual <br> fluency |  |  | Recall the 10 and 5 <br> multiplication tables, <br> and corresponding <br> division facts. | Recall the 3,6 and 9 <br> multiplication tables, <br> and corresponding <br> division facts. | Secure and maintain <br> fluency in all <br> multiplication tables, <br> and corresponding <br> division facts, <br> through continued <br> practice. |
|  |  |  | Recall the 2, 4 and 8 <br> multiplication tables, <br> and corresponding <br> division facts. | Recall the 7 <br> multiplication table, <br> and corresponding <br> division facts. |  |
|  |  |  |  | Recall the 11 and 12 <br> multiplication tables, <br> and corresponding <br> division facts. |  |

# Using concrete and pictorial methods to help learn times tables at home. 

Helping with the laundry! How many
Using play or objectives e.g pair up toys cars and count them
 pairs of socks will I have if there are 20 socks in total?


How many shoes are there?
Count in groups of two.



## $2 \times 3=2+2+2$


2 eggs mutiplied by 3 is the same as adding 2, 3 times.
OO+O+O
OO+O+O
= 6
= 6


Draw/use practical equipment to create arrays

Help to understand that it is repeated Use a number line to help visualise the jumps. addition: $2 \times 3=2$ lots of 3 .


What can you see?


## Arrays are all around us



## 88888

## Year 1 National Curriculum expectations

Solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher.

| 10 | 20 |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |

$\square$


Circle each column of apples.


Use 30 counters.


How many columns are there?
a) Share the counters between 2 friends.


## Year 2 National Curriculum Expectations

- recall and use multiplication and division facts for the 2,5 and 10 multiplication tables, including recognising odd and even numbers
- calculate mathematical statements for multiplication and division within the multiplication tables and write them using the multiplication $(\times)$, division ( $\div$ ) and equals (=) signs
- show that multiplication of two numbers can be done in any order (commutative) and division of one number by another cannot
- solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts.

| Addition | Multiplication |
| :---: | :---: |
| $2+2+2+2$ | $4 \times 2$ |
| $5+5+5$ |  |
| $3+3+3+3+3$ |  |
|  | $2 \times 10$ |



## Year 2 - what does this look <br> like

a) Match the picture to the times-table fact.

$1 \times 5$
$5 \times 5$
$2 \times 5$


Complete the number sentences for each array
a)

b)


Is there another way to work this out?
https://www.bbc.co.uk/cbeebies/shows/numberblocks

https://www.bbc.co.uk/cbeebies/watch/numberblocks-ten-times-table-song

## Year 3- National Curriculum Expectations

- recall and use multiplication and division facts for the 3,4 and 8 multiplication tables
- write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods
- solve problems, including missing number problems, involving multiplication and division, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects.


## Year 3 - what does this

## look like

| Tens | Ones |
| :---: | :---: |
| Wmmmm | E E E |
| \|m1711 | - E |
| Wmmmm | - $\mathrm{B}^{\text {E }}$ |
|  | - E |
|  | - $\mathrm{E}^{-1}$ |

How many marbles are there in total?



Work out the missing values in each bar model.
a)

b)


| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |

What two patterns do you notice?
a) Amir draws 7 jumps of 8 on a number line.


Explain how you worked it out.


- https://whiterosemaths.com/maths-with-michael



## Maths with Michael: Parent's guide to division



## Year 4 - National Curriculum Expectations

- recall multiplication and division facts for multiplication tables up to $12 \times$ 12
- use place value, known and derived facts to multiply and divide mentally, including: multiplying by 0 and 1 ; dividing by 1 ; multiplying together three numbers
- recognise and use factor pairs and commutativity in mental calculations
- multiply two-digit and three-digit numbers by a one-digit number using formal written layout
- solve problems involving multiplying and adding, including using the distributive law to multiply two digit numbers by one digit, integer scaling problems and harder correspondence problems such as n objects are connected to mobjects.


## Year 4 - what does this look like


(1)

$0 \times 3=\square$
$1 \times 3=3$
$2 \times 3=6$
$3 \times 3=9$

| H | T | $\bigcirc$ |
| :---: | :---: | :---: |
| (10) (10) | (1) | (1)(1) |
|  |  | (1) (1) |
| (10) 100 | (1) | (1)(1) |
|  |  | (1) |
| (10) 30 | (1) | (1)(1) |
|  |  | (1) 1 |




## Year 5- National Curriculum Expectations

- identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers
- know and use the vocabulary of prime numbers, prime factors and composite (non prime) numbers
- establish whether a number up to 100 is prime and recall prime numbers up to 19
- multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers
- multiply and divide numbers mentally drawing upon known facts
- divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context
- multiply and divide whole numbers and those involving decimals by 10, 100 and 1000


## Year 5 - what does this look like


a) $52 \times \square=5,200$
b) $95 \times$ $\square$ $=950$
c) $136 \times$ $\qquad$ $=1,360$
f) $\square \times 370=3,700$
g) $\square \times 100=8,200$
h) $\square \times 100=82,000$

$7 \times 10$
$39 \times 10$
$205 \times 10$


\[

\]



| $b$ | $b$ | $b$ | $b$ | $b$ |  | $b$ | $b$ | $b$ | b |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5,328 |  |  |  |  |  |  |  |  |  |

## Year 6- National Curriculum Expectations

- multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication
- divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context
- divide numbers up to 4 digits by a two-digit number using the formal written method of short division where appropriate, interpreting remainders according to the context
- perform mental calculations, including with mixed operations and large numbers
- identify common factors, common multiples and prime numbers
- use their knowledge of the order of operations to carry out calculations involving the four operations
- solve problems involving addition, subtraction, multiplication and division
- use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy.


## Year 6 - what does this look like


!


1) Which is the best estimate to use to check the answer to $488 \times 32$ ?

$$
500 \times 40
$$

$400 \times 30$
$500 \times 30$
2) $12 \times 6=72$
3) $1,200 \times 6=7,200$
4) $12 \times 600=7,200$

## End Points

## 2019 Arithmetic Paper: Multiplication and Division

- $9 \times 41=\quad \cdot 101 \times 1,000=$
- $180 \div 3=$
- $20 \%$ of $3000=$
- $120 \div 12=$
- $0.9 \div 100=$
- $213 \times 0=$
- $91 \div 7=$
- $1210 \div 11=$
- $25.34 \times 10=$
- $60 \div(30-24)=$
- $3^{3}=$
- $836 \times 27=$
- $888 \div 37=$
- $35 \%$ of $320=$
- $51 \%$ of $900=$
- $3468 \times 62=$
- $36 \%$ of $450=$
- $8051 \div 83=$


## White Rose - Small Step Approach

- Each block is broken down into a series of small learning steps. Together, these small steps cover all the curriculum content that your child needs to know.
- Your child will remember more by learning maths in small, related chunks

Step 2 Make equal groups

Step 3 Add equal groups

Step 4 Introduce the multiplication symbol

Step 5 Multiplication sentences

Step 6 Use arrays

Step 7 Make equal groups - grouping

Step 8 Make equal groups - sharing

Step 9 The 2 times-table

Step 10 Divide by 2

Step 11 Doubling and halving

Step 12 Odd and even numbers

Step 13 The 10 times-table

Step 14 Divide by 10

Step 15 The 5 times-table

## Mathematical Vocabulary

| Multiplication <br> An operation that finds the total of repeated equal groups (Repeated addition) | Factore <br> The numbers that are being mult pied together |
| :---: | :---: |
| $5 \times 4=20$ <br> The answer to a multiplication equation | All the products of a certain number. (Example $\times 10$ ) |


| Division | Divisor$20 \div 5=4$ |
| :---: | :---: |
| D. Andindin |  |
|  |  |
| Dividend | Quotient |
| $20 \div 5=4$ | $20 \div 5=4$ |
|  |  |

Prime Numbers
$\qquad$


Square Numbers


## Fluency, reasoning and problem solving skills

## What is fluency?

Fluency starts with the ability to apply procedures accurately and efficiently. This means that children quickly become confident in the methods they will later need to use to solve more complex problems.

## What is reasoning?

Reasoning enables children to make use of all their other mathematical skills; it could be described as the glue that helps mathematics make sense. Reasoning is children understanding mathematics well enough that they can apply it to new situations and explain it.

## What is problem solving?

Problem solving is applying the mathematics children have learnt to solve problems. If children are fluent in the mathematical procedures required for each topic, problem solving becomes much easier. When approaching problems, children must first work out what the problem is asking them to do, before then applying their procedural knowledge to find a solution.

## Using and applying these multiplication and division skills




> Year Three



A pattern is made up of regular octagons that are all the same size.


The perimeter of the whole pattern is 640 cm .
What is the perimeter of each octagon?


Eva is thinking of a number.

1 multiply it by 6
then multiply the answer
by 8 , then subtract 500 .
The result is 9,100

What number did Eva start with?

## Correct or Incorrect?

| Example A: |
| ---: |
| 240 |
| 143514 <br> 28 <br> 71 <br> 70 <br> 14 <br> 14 <br> 0 |

Example B:
342
$1 4 \longdiv { 4 7 8 8 }$ $42 \downarrow$
56
$\begin{array}{r}28 \\ \hline 0\end{array}$

Explain the mistakes.

## Multiplication Check - End of Year Four

## Information for parents:

2023 multiplication tables check


The purpose of the check is to determine whether your child can fluently recall their times tables up to 12 , which is essential for future success in mathematics.

It is an on-screen check consisting of 25 times table questions.
They will then have 6 seconds to answer each question. On average, the check should take no longer than 5 minutes to complete.
https://mathsframe.co.uk/en/resources/resource/477/Multipli cation-Tables-Check
https://ttrockstars.com
Lattachment data/file/1116420/2023 Information for parents Multiplicatio n tables check Nov 22 PDFA.pdf

## Multiplication and division facts

The full set of multiplication calculations that pupils need to be able to solve by automatic recall are shown in the table below. Pupils must also have automatic recall of the corresponding division facts.

| $1 \times 1$ | $1 \times 2$ | $1 \times 3$ | $1 \times 4$ | $1 \times 5$ | $1 \times 6$ | $1 \times 7$ | $1 \times 8$ | $1 \times 9$ | $1 \times 10$ | $1 \times 11$ | $1 \times 12$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $2 \times 1$ | $2 \times 2$ | $2 \times 3$ | $2 \times 4$ | $2 \times 5$ | $2 \times 6$ | $2 \times 7$ | $2 \times 8$ | $2 \times 9$ | $2 \times 10$ | $2 \times 11$ | $2 \times 12$ |
| $3 \times 1$ | $3 \times 2$ | $3 \times 3$ | $3 \times 4$ | $3 \times 5$ | $3 \times 6$ | $3 \times 7$ | $3 \times 8$ | $3 \times 9$ | $3 \times 10$ | $3 \times 11$ | $3 \times 12$ |
| $4 \times 1$ | $4 \times 2$ | $4 \times 3$ | $4 \times 4$ | $4 \times 5$ | $4 \times 6$ | $4 \times 7$ | $4 \times 8$ | $4 \times 9$ | $4 \times 10$ | $4 \times 11$ | $4 \times 12$ |
| $5 \times 1$ | $5 \times 2$ | $5 \times 3$ | $5 \times 4$ | $5 \times 5$ | $5 \times 6$ | $5 \times 7$ | $5 \times 8$ | $5 \times 9$ | $5 \times 10$ | $5 \times 11$ | $5 \times 12$ |
| $6 \times 1$ | $6 \times 2$ | $6 \times 3$ | $6 \times 4$ | $6 \times 5$ | $6 \times 6$ | $6 \times 7$ | $6 \times 8$ | $6 \times 9$ | $6 \times 10$ | $6 \times 11$ | $6 \times 12$ |
| $7 \times 1$ | $7 \times 2$ | $7 \times 3$ | $7 \times 4$ | $7 \times 5$ | $7 \times 6$ | $7 \times 7$ | $7 \times 8$ | $7 \times 9$ | $7 \times 10$ | $7 \times 11$ | $7 \times 12$ |
| $8 \times 1$ | $8 \times 2$ | $8 \times 3$ | $8 \times 4$ | $8 \times 5$ | $8 \times 6$ | $8 \times 7$ | $8 \times 8$ | $8 \times 9$ | $8 \times 10$ | $8 \times 11$ | $8 \times 12$ |
| $9 \times 1$ | $9 \times 2$ | $9 \times 3$ | $9 \times 4$ | $9 \times 5$ | $9 \times 6$ | $9 \times 7$ | $9 \times 8$ | $9 \times 9$ | $9 \times 10$ | $9 \times 11$ | $9 \times 12$ |
| $10 \times 1$ | $10 \times 2$ | $10 \times 3$ | $10 \times 4$ | $10 \times 5$ | $10 \times 6$ | $10 \times 7$ | $10 \times 8$ | $10 \times 9$ | $10 \times 10$ | $10 \times 11$ | $10 \times 12$ |
| $11 \times 1$ | $11 \times 2$ | $11 \times 3$ | $11 \times 4$ | $11 \times 5$ | $11 \times 6$ | $11 \times 7$ | $11 \times 8$ | $11 \times 9$ | $11 \times 10$ | $11 \times 11$ | $11 \times 12$ |
| $12 \times 1$ | $12 \times 2$ | $12 \times 3$ | $12 \times 4$ | $12 \times 5$ | $12 \times 6$ | $12 \times 7$ | $12 \times 8$ | $12 \times 9$ | $12 \times 10$ | $12 \times 11$ | $12 \times 12$ |

Pupils must be fluent in these facts by the end of year 4, and this is assessed in the multiplication tables check. Pupils should continue

## Useful Websites to support children's Maths skills

https://www.bbc.co.uk/cbeebies/grownups/help-your-child-with-maths - have lots of fun and interactive games and activities to help get our younger children excited about Maths

Hit the Button (https://www.topmarks.co.uk/maths-games/hit-the-button)

- children love this game as it helps to increase confidence through practising times tables and number bonds.
https://mathszone.co.uk/ - this site is jam-packed with fun ways to learn more about maths.
https://www.bbc.co.uk/bitesize/subjects/z826n39 - lots of information alongside short videos help to make the learning enjoyable and accessible for all children.
https://www.transum.org/Software/Fun Maths/ - KS2 challenges
https://wild.maths.org/ - KS2 challenges
https://whiterosemaths.com/parent-resources - free printable workbooks

https://ttrockstars.com/ Games for all - (Year 1-6) have an account (TT Rockstars and Numbots)
https://whiterosemaths.com/resources/1-minute-maths - free app to download
https://www.mymaths.co.uk/ - Year $1-6$ have an account
https://play.edshed.com/en-gb - Mathshed (same password as Spellingshed)

(88) MyMaths



## TT Rockstars

Checking your child's progress is easy:
When your child has logged in, select their avatar in the top right hand corner and then select the ' My Stats' option.
In the effort tab, you can see how many minutes the children have played.

Under fluency, you can see how quickly your child is able to answer each question and how confident they are with their individual times table knowledge.

The URL on the right will help show you this process in more detail


## Learners with different needs

| How can I hide the timer? | Start a game and press <br> in Jamming. |
| :--- | :--- |
| How can I increase the <br> length of Garage games? | Single player > Garage > press the little arrow below "play solo" <br> > choose 1,2 or 3 minutes. |
| The tables are too hard | Make sure your child is playing in Garage or Arena game modes. If this does <br> not resolve the issue, please speak to your child's teacher. Remember that <br> Jamming mode allows the child to choose the tables themselves. |
| My child gets anxious | Try the three above plus: setting mini goals (e.g. complete 2 minutes today, <br> get 1 more point in the next game, pass 1 level); having a break from online <br> play (come back in a couple of days); and reminding them of Baz's words: <br> "A good rock star stays chillaxed by accepting they make mistakes." |
| My child has visual | Head to the Profile page where you can: change the colour scheme; reduce <br> the visual stimuli with Declutter mode; increase the font size or switch to a <br> impairments; what <br> dyslexia-friendly font called Lexie. play.ttrockstars.com is also screen reader <br> compatible. |
| settings are available? | Yes in Jamming mode but not in the other games. The reason for that is that <br> practising multiplication and division at the same time supports the recall of <br> both and is the most successful approach. If your child is finding division <br> confusing, please speak to their teacher about starting with the 10 s only and <br> for advice on how to help at home. |
| Can I turn off division? |  |

## Super Fingers!

This is a game for two players!
The game is basically a version of rock, paper, scissors but with numbers. Two players count to 3 and then make a number using their fingers.

Both players then have to multiply both numbers together and the quickest wins.


You can:

- Adapt other games to focus on multiplication tables, or create some totally new tables games with your child.
- Start the game by giving children a copy of the times table to refer to if they need it. Then, when they're ready for the challenge, they can try the game without.


## 9 Times Tables on your Fingers!

1. Hold your hands in front of you with your fingers spread out.
2. For $9 \times 4$ bend your 4 th finger down llike the
 picture).
3. You have 3 fingers in front of the bent finger and 6 after the bent finger. Thus the answer must be 36!
4. The technique works for the 9 times table up to 10 .

## You can:

- Explore with your child which method helps them most with the 9 times table - the more physical hand trick, or the more visual exploration of number patterns.


## Bingo!

This game will need 2 players!
Make a grid of six squares on a piece of paper and ask your child to write a number in each square from the target tables. Give them a question and if they have the answer, they mark them off. First one to mark off all their numbers is the winner!


## You can:

- Turn this into a family game and include a reasonable reward/incentive to entice your child.


## Four Facts

Use the three numbers in the bubbles to make four facts.


## How can you help your child with Maths at home?

Take away their fear.
Reassure and praise whenever possible. Positive mindset...
Let them see you using Maths in your everyday routines - portioning meals between the family, chopping vegetables into halves and quarters etc.
Seeing mistakes as an opportunity to learn and using them as a discussion point.
Recognising the importance and value of Maths in our everyday lives e.g. managing money and telling the time

